

# CLAIMS

1-27. (Cancelled)

28. (New) A method of determining a position estimate based on an updated Kalman filter, comprising:

receiving a first measurement  $L_1$  based on a first signal with wavelength  $\lambda_1$  and

frequency  $f_1$ ;

receiving a second measurement  $L_2$  based on a second signal with wavelength  $\lambda_2$

and frequency  $f_2$ ;

selecting a model  $\alpha$  of distance dependent and distance independent errors in the

first and second measurements, wherein the model  $\alpha$  is selected from  $\alpha =$

$\lambda_1/\lambda_2$ ,  $\alpha = \lambda_2/\lambda_1$ , and  $\alpha = 1$ ;

based on the model  $\alpha$ , calculating a double differenced variance matrix:

$$D(L_1, L_2) = \begin{bmatrix} D_{11} & 0 \\ 0 & \bar{D}_{22} \end{bmatrix};$$

wherein

$$D_{11} = 2R_{L2}^2 \begin{bmatrix} W_1 + W_{ref} & W_{ref} & \dots & W_{ref} & W_{ref} \\ W_{ref} & W_2 + W_{ref} & \dots & W_{ref} & W_{ref} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ W_{ref} & W_{ref} & \dots & W_{n-2} + W_{ref} & W_{ref} \\ W_{ref} & W_{ref} & \dots & W_{ref} & W_{n-1} + W_{ref} \end{bmatrix};$$

wherein

$$\overline{D}_{22} = (R_{L2}^2 + \alpha^2 R_{L1}^2 - 2\alpha R_{L1,L2}) \begin{bmatrix} W_1 + W_{ref} & W_{ref} & \dots & W_{ref} & W_{ref} \\ W_{ref} & W_2 + W_{ref} & \dots & W_{ref} & W_{ref} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ W_{ref} & W_{ref} & \dots & W_{n-2} + W_{ref} & W_{ref} \\ W_{ref} & W_{ref} & \dots & W_{ref} & W_{n-1} + W_{ref} \end{bmatrix};$$

wherein

$$R_{L1} = \left( \frac{1}{\lambda_1^2} [R_{non-dist,L1}^2 + (R_{ion}^2 + R_{trop}^2 + R_{orb}^2) \cdot B^2] \right)^{\frac{1}{2}};$$

wherein

$$R_{L2} = \left( \frac{1}{\lambda_2^2} [R_{non-dist,L2}^2 + (R_{ion}^2 + R_{trop}^2 + R_{orb}^2) \cdot B^2] \right)^{\frac{1}{2}};$$

wherein

$$R_{L1,L2} = \frac{1}{\lambda_1 \lambda_2} (R_{ion}^2 + R_{trop}^2 + R_{orb}^2) \cdot \left( \int_1^4 R_{ion}^2 + R_{trop}^2 + R_{orb}^2 \cdot B^2 \right);$$

wherein  $R_{non-dist,L1}$  is a non-distance dependant measurement error for the  $L_1$  measurement;

wherein  $R_{non-dist,L2}$  is a non-distance dependant measurement error for the  $L_2$  measurement;

wherein  $R_{ion}$  is measurement error due to ionospheric delay;

wherein  $R_{trop}$  is measurement error due to tropospheric delay;

wherein  $R_{orb}$  is measurement error due to orbit bias;

wherein each W is:  $W_n = 1.0 + 7.5e^{-E/15}$ ;

wherein n is a satellite ordinal of a plurality of satellites;

wherein  $W_{ref}$  corresponds to a reference satellite of the plurality of satellites;

wherein E is the elevation angle of each satellite of the plurality of satellites;

updating a Kalman filter with the calculated variance matrix; and

determining a present position estimate based on the updated Kalman filter.

29. (New) The method of claim 28, wherein the updated Kalman filter with the calculated variance matrix is  $K = D(L_1, L_2)_{new} H_2^T \{H_2^T D(L_1, L_2)_{new} H_2^T + V_2\}^{-1}$ ;

wherein  $H_2^T$  is a transpose of a design matrix  $H_2$  for the measurement  $L_2$ ;

wherein  $V_2$  is a residual measurement of measurement  $L_2$ ;

wherein  $D(L_1, L_2)_{new} = D(L_1, L_2)_{old} - K_{old} H_2 D(L_1, L_2)_{old}$ ;

wherein  $D(L_1, L_2)_{new}$  is the calculated variance matrix including the received measurements  $L_1$  and  $L_2$ ;

wherein  $D(L_1, L_2)_{old}$  is a previous calculated variance matrix which was calculated before receiving both of the received measurements  $L_1$  and  $L_2$ ; and

wherein  $K_{old}$  is a previous Kalman filter which was calculated before receiving both of the received measurements  $L_1$  and  $L_2$ .

30. (New) A computer readable medium having computer-executable instructions, comprising:

receiving a first measurement  $L_1$  based on a first signal with wavelength  $\lambda_1$  and frequency  $f_1$ ;

receiving a second measurement  $L_2$  based on a second signal with wavelength  $\lambda_2$  and frequency  $f_2$ ;

selecting a model  $\alpha$  of distance dependent and distance independent errors in the

first and second measurements, wherein the model  $\alpha$  is selected from  $\alpha =$

$\lambda_1/\lambda_2$ ,  $\alpha = \lambda_2/\lambda_1$ , and  $\alpha = 1$ ;

based on the model  $\alpha$ , calculating a double differenced variance matrix:

$$D(L_1, L_2) = \begin{vmatrix} D_{11} & 0 \\ 0 & \overline{D}_{22} \end{vmatrix};$$

wherein

$$D_{11} = 2R_{L2}^2 \begin{vmatrix} W_1 + W_{ref} & W_{ref} & \dots & W_{ref} & W_{ref} \\ W_{ref} & W_2 + W_{ref} & \dots & W_{ref} & W_{ref} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ W_{ref} & W_{ref} & \dots & W_{n-2} + W_{ref} & W_{ref} \\ W_{ref} & W_{ref} & \dots & W_{ref} & W_{n-1} + W_{ref} \end{vmatrix};$$

wherein

$$\overline{D}_{22} = (R_{L2}^2 + \alpha^2 R_{L1}^2 - 2\alpha R_{L1,L2}) \begin{vmatrix} W_1 + W_{ref} & W_{ref} & \dots & W_{ref} & W_{ref} \\ W_{ref} & W_2 + W_{ref} & \dots & W_{ref} & W_{ref} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ W_{ref} & W_{ref} & \dots & W_{n-2} + W_{ref} & W_{ref} \\ W_{ref} & W_{ref} & \dots & W_{ref} & W_{n-1} + W_{ref} \end{vmatrix};$$

wherein

$$R_{L1} = \left( \frac{1}{\lambda_1^2} [R_{non-dist,L1}^2 + (R_{ion}^2 + R_{trop}^2 + R_{orb}^2) \cdot B^2] \right)^{\frac{1}{2}};$$

wherein

$$R_{L2} = \left( \frac{1}{\lambda_2^2} [R_{non-dist,L2}^2 + (R_{ion}^2 + R_{trop}^2 + R_{orb}^2) \cdot B^2] \right)^{\frac{1}{2}};$$

wherein

$$R_{L1,L2} = \frac{1}{\lambda_1 \lambda_2} (R_{ion}^2 + R_{trop}^2 + R_{orb}^2) \cdot \left( \frac{f_1^4}{f_2^4} R_{ion}^2 + R_{trop}^2 + R_{orb}^2 \right) \cdot B^2;$$

wherein  $R_{non-dist,L1}$  is a non-distance dependant measurement error for the

$L_1$  measurement;

wherein  $R_{non-dist,L2}$  is a non-distance dependant measurement error for the

$L_2$  measurement;

wherein  $R_{ion}$  is measurement error due to ionospheric delay;

wherein  $R_{trop}$  is measurement error due to tropospheric delay;

wherein  $R_{orb}$  is measurement error due to orbit bias;

wherein each  $W$  is:  $W_n = 1.0 + 7.5e^{-E/15}$ ;

wherein  $n$  is a satellite ordinal of a plurality of satellites;

wherein  $W_{ref}$  corresponds to a reference satellite of the plurality of satellites;

wherein  $E$  is the elevation angle of each satellite of the plurality of satellites;

updating a Kalman filter with the calculated variance matrix; and

determining a present position estimate based on the updated Kalman filter.

31. (New) The computer readable medium of claim 31, wherein the updated Kalman filter with the calculated variance matrix is:

$$K = D(L_1, L_2)_{new} H_2^T \{H_2^T D(L_1, L_2)_{new} H_2 + V_2\}^{-1};$$

wherein  $H_2^T$  is a transpose of a design matrix  $H_2$  for the measurement  $L_2$ ;

wherein  $V_2$  is a residual measurement of measurement  $L_2$ ;

wherein  $D(L_1, L_2)_{new} = D(L_1, L_2)_{old} - K_{old} H_2 D(L_1, L_2)_{old}$ ;

wherein  $D(L_1, L_2)_{new}$  is the calculated variance matrix including the received measurements  $L_1$  and  $L_2$ ;

wherein  $D(L_1, L_2)_{old}$  is a previous calculated variance matrix which was  
calculated before receiving both of the received measurements  $L_1$  and  $L_2$ ;  
and

wherein  $K_{old}$  is a previous Kalman filter which was calculated before receiving  
both of the received measurements  $L_1$  and  $L_2$ .